

Fermi Level location of Intrinsic Semiconductor

The location of the Fermi level is a function of the carrier concentration. We will use Eqs. (4) and (5) to identify the Fermi level.

For intrinsic semiconductor, $n_o = p_o$

$$N_c \cdot \exp\left(\frac{-(E_c - E_F)}{kT}\right) = N_v \cdot \exp\left(\frac{-(E_F - E_v)}{kT}\right)$$
$$E_F = \frac{1}{2}(E_c + E_v) + \frac{1}{2}kT \ln\left(\frac{N_v}{N_c}\right) \dots \dots \dots (9)$$

Because $N_c = 2 \left(\frac{2\pi m_n^* k T}{h^2}\right)^{3/2}$ and $N_v = 2 \left(\frac{2\pi m_p^* k T}{h^2}\right)^{3/2}$

Equation (9) becomes:

$$E_F = \frac{1}{2}(E_c + E_v) + \frac{3}{4}kT \ln\left(\frac{m_p^*}{m_n^*}\right) \dots \dots \dots (10)$$

The term $\frac{1}{2}(E_c + E_v)$ is midgap energy. Eq.(10) rewrite:

$$E_F = E_{\text{midgap}} + \frac{3}{4}kT \ln\left(\frac{m_p^*}{m_n^*}\right) \dots \dots \dots (11)$$

Example: Where is E_F located in the energy band of silicon, at 300K with $n_o=10^{17}$ cm^{-3} ? And for $p_o = 10^{14} \text{cm}^{-3}$?

The values of $N_c = 2.8 \times 10^{19} \text{cm}^{-3}$ and $N_v = 1.04 \times 10^{19} \text{cm}^{-3}$.

Solution:

$$n_o = N_c \cdot \exp\left(\frac{-(E_c - E_F)}{kT}\right)$$

$$E_c - E_F = kT \cdot \ln \left(\frac{N_c}{n_o} \right) = 0.026 \ln \left(\frac{2.8 \times 10^{19}}{10^{17}} \right) = 0.146 \text{ eV}$$

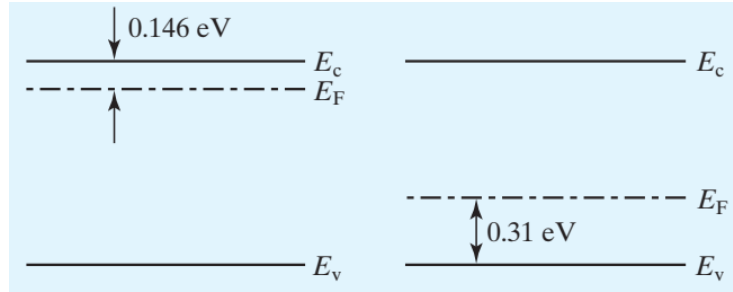
Therefore, E_F is located at 146 meV below E_c , as shown in Figure.

For $p_o = 10^{14} \text{ cm}^{-3}$,

$$p_o = N_v \cdot \exp \left(\frac{-(E_F - E_v)}{kT} \right)$$

$$E_F - E_v = kT \cdot \ln \left(\frac{N_v}{p_o} \right) = 0.026 \ln \left(\frac{1.04 \times 10^{19}}{10^{14}} \right) = 0.31 \text{ eV}$$

Therefore E_F is located at 0.31 eV above E_v .



Thermal Motion of Electrons and Holes

Even without an applied electric field, carriers are not at rest but possess finite kinetic energies. The **average kinetic energy of electrons** is

$$\text{The average kinetic energy of electron} = \frac{\text{total kinetic energy}}{\text{number of electrons}}$$

$$= \frac{\int_{E_c}^{top} g_c(E) f(E) (E - E_c) dE}{\int_{E_c}^{top} g_c(E) f(E) dE} \dots \dots \dots (1)$$

After solving Eq. (1), the result is

$$\text{Average kinetic energy} = \frac{3}{2}kT \dots\dots\dots (2)$$

Eq. (2) is true for both electrons and holes. The kinetic energy of electrons or holes can be used in Eq. (2),

$$\frac{1}{2}m^*v_{th}^2 = \frac{3}{2}kT \dots\dots\dots (3)$$

So, the thermal velocity (v_{th}) can be written:

$$v_{th} = \sqrt{\frac{3kT}{m^*}} \dots\dots\dots (4)$$

where m^* is the effective mass of electron / hole.

Example: What are the approximate thermal velocities of electrons and holes in silicon at room temperature? $m_e^* = 0.26 m_o$ and $m_h^* = 0.39 m_o$

Solution:

$$\text{For the electrons, } v_{th} = \sqrt{\frac{3kT}{m^*}} = \sqrt{\frac{3 \times (1.38 \times 10^{-23} \frac{J}{K}) \times (300 \text{ K})}{0.26 \times 9.1 \times 10^{-31} \text{ kg}}} = 2.3 \times 10^5 \text{ m/s}$$

$$\text{For the holes, } v_{th} = \sqrt{\frac{3kT}{m^*}} = \sqrt{\frac{3 \times (1.38 \times 10^{-23} \frac{J}{K}) \times (300 \text{ K})}{0.39 \times 9.1 \times 10^{-31} \text{ kg}}} = 2.2 \times 10^5 \text{ m/s}$$

Note 1: $1 \text{ J} = 1 \text{ kg.m}^2/\text{s}^2$

Note 2: The typical thermal velocity of electrons and holes is about 1000 times slower than the speed of light and 100 times faster than the sonic speed.